

Name: _____
AP Calculus AB

Date: _____
Ms. Loughran

Do Now:

1. If $f(0) = 3$ and $f(x) = \sqrt{9 + \sin(2x)}$, then estimate the value of $f(0.06)$ using local linearization.

2. $\int (1 - \cos^2 x \sec x) dx =$ } we did in open review on Wednesday

3. $\int ((x^2 + 2)(1 - x)) dx =$

$$\textcircled{1} f'(x) = \frac{1}{2} (9 + \sin(2x))^{-\frac{1}{2}} \cdot 2 \cos 2x$$

$$f'(0) = (9 + \sin 0)^{-\frac{1}{2}} \cdot \cos 0$$

$$9^{-\frac{1}{2}} \cdot 1 = \frac{1}{3}$$

$$y - 3 = \frac{1}{3}x$$

$$y = \frac{1}{3}x + 3$$

$$y = \frac{1}{3}(\overset{.02}{\cancel{0.06}}) + 3 = 3.02$$

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Fundamental Theorem of Calculus Part I:

If a function f is continuous on an interval $[a,b]$, then it follows that

$$\int_a^b f(x) dx = F(b) - F(a) \text{ where } F \text{ is a function such that } F'(x) = f(x)$$

(F is any antiderivative of f).

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AP Calculus AB Evaluating Definite Integrals

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Part A. Directions: Answer these questions *without* using your calculator.

1. $\int_{-1}^1 (x^2 - x - 1) dx =$

- (A) $\frac{2}{3}$ (B) 0 (C) $-\frac{4}{3}$ (D) -2 (E) -1

$$\left. \begin{array}{l} \frac{x^3}{3} - \frac{x^2}{2} - x \\ -1 \end{array} \right|_1$$

$$\frac{1^3}{3} - \frac{1^2}{2} - 1 - \left(\frac{(-1)^3}{3} - \frac{(-1)^2}{2} - (-1) \right)$$

$$\frac{1}{3} - \frac{1}{2} - 1 - \left(-\frac{1}{3} - \frac{1}{2} + 1 \right)$$

$$\frac{1}{3} - \frac{1}{2} - 1 + \frac{1}{3} + \frac{1}{2} - 1 = \frac{2}{3} - 2 = -\frac{4}{3}$$

2. $\int_1^2 \frac{3x-1}{3x} dx =$

- (A) $\frac{3}{4}$ (B) $1 - \frac{1}{3} \ln 2$ (C) $1 - \ln 2$ (D) $-\frac{1}{3} \ln 2$ (E) 1

$$\int_1^2 \left(1 - \frac{1}{3}x^{-1} \right) dx$$

$$\left. x - \frac{1}{3} \ln|x| \right|_1^2$$

$$2 - \frac{1}{3} \ln|2| - \left(1 - \frac{1}{3} \ln|1| \right)$$

$$2 - \frac{1}{3} \ln 2 - 1 + \frac{1}{3} \ln 1$$

$$2 - \frac{1}{3} \ln 2 - 1 + 0$$

$$1 - \frac{1}{3} \ln 2$$

3. $\int_0^3 \frac{dt}{\sqrt{4-t}} =$

- (A) 1 (B) -2 (C) 4 (D) -1 (E) 2

$u = 4 - t$

$du = -dt$

$-du = dt$

$-\int_{4-0}^{4-3} u^{-\frac{1}{2}} du$

$-\int_4^1 u^{-\frac{1}{2}} du = -2u^{\frac{1}{2}} \Big|_4^1 = -2(1)^{\frac{1}{2}} - (-2(4)^{\frac{1}{2}})$
 $= -2 - (-4)$

4. $\int_{-1}^0 \sqrt{3u+4} du =$

- (A) 2 (B) $\frac{14}{9}$ (C) $\frac{14}{3}$ (D) 6 (E) $\frac{7}{2}$

$y = 3u + 4$

$dy = 3 du$

$\frac{dy}{3} = du$

$\frac{1}{3} \int_{3(-1)+4}^{3(0)+4} y^{\frac{1}{2}} dy = \frac{1}{3} \int_1^4 y^{\frac{1}{2}} dy = \frac{1}{3} \cdot \frac{2}{3} y^{\frac{3}{2}} \Big|_1^4$

$\frac{2}{9} y^{\frac{3}{2}} \Big|_1^4$

$\frac{2}{9} (4^{\frac{3}{2}} - 1^{\frac{3}{2}}) = \frac{2}{9} (8 - 1) = \frac{14}{9}$

5. $\int_2^3 \frac{dy}{2y-3} =$

- (A) $\ln 3$ (B) $\frac{1}{2} \ln \frac{3}{2}$ (C) $\frac{16}{9}$ (D) $\ln \sqrt{3}$ (E) $\sqrt{3} - 1$

$u = 2y - 3$

$du = 2dy$

$\frac{du}{2} = dy$

$\frac{1}{2} \int_{2(2)-3}^{2(3)-3} \frac{1}{u} du$

$\frac{1}{2} \int_1^3 \frac{1}{u} du = \frac{1}{2} \ln|u| \Big|_1^3$

$\frac{1}{2} (\ln 3 - \ln 1) = \frac{1}{2} \ln 3$
 $\ln 3^{\frac{1}{2}}$
 $\ln \sqrt{3}$

6. $\int_0^{\sqrt{3}} \frac{x}{\sqrt{4-x^2}} dx =$

- (A) 1 (B) $\frac{\pi}{6}$ (C) $\frac{\pi}{3}$ (D) -1 (E) 2

$u = 4 - x^2$

$du = -2x dx$

$-\frac{du}{2} = x dx$

$-\frac{1}{2} \int_{4-0^2}^{4-(\sqrt{3})^2} u^{-\frac{1}{2}} du$

$-\frac{1}{2} \int_4^1 u^{-\frac{1}{2}} du = -\frac{1}{2} \left[2u^{\frac{1}{2}} \right]_4^1$

$-\frac{1}{2} \left[1^{\frac{1}{2}} - 4^{\frac{1}{2}} \right]$
 $-\frac{1}{2} [1 - 2]$
 $-\frac{1}{2} [-1]$
 $\frac{1}{2}$