

Name: _____
AP Calc AB: Derivatives of Inverse Trig Functions

Date: _____
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Do Now:

1. If $f(x) = \sin^2 3x$, find $f'\left(\frac{\pi}{4}\right)$.

$$f'(x) = 2\sin(3x)\cos(3x) \cdot 3$$

$$f'(x) = 6\sin(3x)\cos(3x)$$

$$f'\left(\frac{\pi}{4}\right) = 6\sin\left(\frac{3\pi}{4}\right)\cos\left(\frac{3\pi}{4}\right)$$

$$= 6\left(\frac{\sqrt{2}}{2}\right)\left(-\frac{\sqrt{2}}{2}\right) = -3$$

2. If $f(x) = 5e^{2x} - 4$, find $f'(\ln 3)$.

$$f'(x) = 5e^{2x} \cdot 2 = 10e^{2x}$$

$$f'(\ln 3) = 10e^{2\ln 3} = 10e^{\ln 3^2} = 10 \cdot 3^2 = 90$$

3. If $f(x) = \sec^2(e^{\cos^2(3x)}) - \tan^2(e^{\cos^2(3x)})$, find $f'\left(\frac{\pi}{4}\right)$.

$$\begin{aligned} & * \tan^2 x + 1 = \sec^2 x * \\ & 1 = \sec^2 x - \tan^2 x \end{aligned}$$

$$f(x) = 1$$

$$f'(x) = 0$$

$$f'\left(\frac{\pi}{4}\right) = 0$$

Exam 2

① $3x - 4y = 0$

$3x = 4y$

$\frac{3}{4}x = y$

$m_{\text{tan}} = \frac{3}{4}$

Q1 $y = x^3 + k, k = ?$

$y' = 3x^2$

$\frac{3}{4} = \frac{3x^2}{1}$

$12x^2 = 3$

$x^2 = \frac{1}{4}$

$x = \pm \frac{1}{2}$

$y = \frac{3}{4} \left(\frac{1}{2}\right) = \frac{3}{8}$

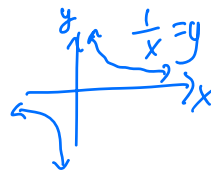
$y = x^3 + k$

$\frac{3}{8} = \left(\frac{1}{2}\right)^3 + k$

$\frac{3}{8} = \frac{1}{8} + k$

$\frac{2}{8} = k$

(B) $\frac{1}{4}$



From somewhere :

$\lim_{x \rightarrow 0} \frac{\sin 4x}{x^2} = \lim_{x \rightarrow 0} \left(\frac{\sin 4x}{x} \cdot \frac{1}{x} \right) = \text{dne}$

Exam 1

④

$f(x) = \begin{cases} \frac{\sqrt{2x+5} - \sqrt{x+7}}{x-2} & x \neq 2 \\ c & x = 2 \end{cases}$

$\lim_{x \rightarrow 2} \left(\frac{\sqrt{2x+5} - \sqrt{x+7}}{x-2} \cdot \frac{(\sqrt{2x+5} + \sqrt{x+7})}{(\sqrt{2x+5} + \sqrt{x+7})} \right)$

$$\lim_{x \rightarrow 2} \frac{2x+5 - (x+7)}{(x-2)(\sqrt{2x+5} + \sqrt{x+7})} \quad (B)$$

$$\lim_{x \rightarrow 2} \frac{1}{\sqrt{2x+5} + \sqrt{x+7}} = \frac{1}{3+3} = \frac{1}{6}$$

$$(3) \quad h(x) = \begin{cases} 3x^2 - 2 & x < -1 \\ f(x) & x \geq -1 \end{cases}$$

$$f(x) = 3(-1)^2 - 2 = 1$$

$$f(x) = 1 \quad @ \quad x = -1$$

$$f(-1) = 1$$

$$(A) \quad \begin{array}{l} x^3 - 1 \\ (-1)^3 - 1 \\ -1 - 1 \\ -2 \end{array}$$

$$(B) \quad \begin{array}{l} 2^{x-1} \\ 2^{-1-1} \\ 2^{-2} \end{array}$$

$$(E) \quad \begin{array}{l} \cos(x+1) \\ \cos(-1+1) \\ \cos 0 \\ 1 \end{array}$$

Exam 2

$$(4) f(x) = \frac{x}{\tan x} \quad f'(\frac{\pi}{4})$$

$$f'(x) = \frac{\tan x (1) - x \sec^2 x}{(\tan x)^2} \quad (\frac{2}{\sqrt{2}})^2$$

$$f'(\frac{\pi}{4}) = \frac{\tan(\frac{\pi}{4}) - \frac{\pi}{4} \sec^2(\frac{\pi}{4})}{(\tan \frac{\pi}{4})^2}$$

$$f'(\frac{\pi}{4}) = \frac{1 - \frac{\pi}{4} (2)}{1^2} = 1 - \frac{2\pi}{4} = 1 - \frac{\pi}{2} \quad (E)$$

Exam 3

$$\tan \frac{\pi}{3} = \sqrt{3}$$

$$(11) y = 2 \ln(\csc x) \text{ at } x = \frac{\pi}{3}$$

$$y' = 2 \cdot \frac{1}{\csc x} \cdot -\cancel{\csc x} \cot x = -2 \cot x$$

$$y'(\frac{\pi}{3}) = -2 \cot \frac{\pi}{3} = -2 \left(\frac{1}{\sqrt{3}} \right) = \frac{-2}{\sqrt{3}}$$

$$\begin{array}{l} \uparrow \text{ m tan line} \\ m_{\text{normal}} = + \frac{\sqrt{3}}{2} \quad (A) \end{array}$$

Exam 1

$$\textcircled{2} \lim_{x \rightarrow 0} \left(\frac{1 - \cos x}{2 \sin^2 x} \cdot \frac{1 + \cos x}{1 + \cos x} \right) = \lim_{x \rightarrow 0} \frac{\sin^2 x}{2 \sin^2 x (1 + \cos x)} = \frac{1}{4} \quad (c)$$

$$\frac{1 - \cos x}{2(1 - \cos^2 x)} = \frac{1 - \cos x}{2(1 - \cos x)(1 + \cos x)}$$