Name: $\qquad$ Date: $\qquad$
AP Calculus AB Using Graphs of Derivatives
1.

The graphs ( $\mathbf{i}$, (ii), and (iii) given below are the graphs of a function $f$ and its first two derivatives $f^{\prime}$ and $f^{\prime \prime}$ (though not necessarily in that order) Identify which of these graphs is the graph of $f$, which is that of $f^{\prime}$ and which is that of $f^{\prime \prime}$. Justify your answer.

2.

The graph below is the graph of the derivative of a function $f$. Use this graph to answer the following questions about. $f$ on the interval $(0,10)$. In each case be sure to justify your answer.

a. On what subinterval(s) is $f$ increasing? $(2,6) \cup(8,10)$
b. On what subinteryal(s) is fore decreasing? $(0,2),(6,8)$
c. Find the $x^{f}$-coordinates of all relative minima of $f . x=2,8 \mathrm{blc}$
d. Find the $x$-coordinates of all relative those values $x=b \quad b / c$
e. On what, subinterval(s) is $f$, concave up?
f. $f^{16}$ th hat subinteryar (k) is concave down?
g. Find the $x$-coordinates of an points of inflection of $f . x=4,7,9$

- to - $\downarrow \nearrow$

$$
\text { (a) } f^{\prime \prime}(x)+0-
$$



(c)


(1) Let the graph in (d) be that of $y=h(x)$.

Which of the others is the graph of $y=h^{\prime}(x)$ ? $k(X)$
(2) Which is the graph of $y=f^{\prime}(x)$ ? $h(x)$
(3) Which is the graph of $y=g^{\prime}(x)$ ? $f(x)$
(4) Which is the graph of $y=g^{\prime \prime}(x)$ ? $h(x)$
(s) Which is the graph of $y=g^{\prime \prime \prime}(x)$ ? $k(x)$

CONCLUSIONS ABOUT FUNCTIONS FROM THEIR DERIVATIVES

1. If $f^{\prime}(x)>0$ on the interval $(\mathrm{a} ; \mathrm{b})$, then the function is increasing on ( $\mathrm{a} ; \mathrm{b}$ ).
2. If $f^{\prime}(x)<0$ on the interval $(a, b)$, then the function is decreasing on (as).
3. If $f^{\prime \prime}(x)<0$ on the interval $(\mathrm{a}, \mathrm{b})$, then the function is concave dốwn on $(a, b)$.
4. If $f^{\prime \prime}(x)>0$ on the interval (abb), then the function is concave up on (abb).

A critical point is defined as a point on the graph where the derivative is either equal to zero or does not exist.

If $f^{\prime}(x)$ changes from positive to negative around a critical point c , then there is a relative maximum point at $\mathrm{x}=\mathrm{c}$.

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(10 \mathrm{cat})
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If $f^{\prime}(x)$ changes from negative to positive around a critical point c , then there is a relative minimum point at $x=c$.

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(10 c i 1):
$$

A point of inflection is a point on the graph where either $f^{\prime \prime}(x)=0$ or does not exist, and there is a change of concavity at that point.
Pis concave up al apt p if there is an interval around $p$ so that the curve $(f(x)$ ) lies above the tanguntlineat?

$f$ is wave down at a pt P if there is
arinterval around $p$ so that the cire lies below the tangent line at $P$



The figure above shows the graph of the derivative of a continuous function $f$ for $0 \leq x \leq 4$.
(a) $\binom{\text { For }}{12}^{\text {what value }} \cup(3,4)^{\text {of } x}$ is $f$ increasing? Justify your answer.
(b) For what values of $x$ does $f$ have its relative minimum value? Justify your answer. $x=3 \mathrm{blc} f^{\prime}$ changs sigh from - to $t$
(c) For what values of $x$ does $f$ have its relative maximum value? Justify your answer. $x=2 \mathrm{bl} \mathrm{c}^{\prime}$ chanes sign form + b-
(d) If $f(1)=1$, use your ansers to (a), (b), and (c) to sketch the graph of $f$ for $1 \leq x \leq 4$.


