Name:
PCH: Modeling with Functions Practice Packet 3

Date:
Ms. Loughran

1. A piece of wire 10 m long is cut into two pieces. One piece, of length $x$, is bent into the shape of a square. The other piece is bent into the shape of an equilateral triangle. Express the total area enclosed as a function of $x$.
2. A right triangle has one vertex on the graph of $y=x^{3}, x>0$ at $(x, y)$, another at the origin, and the third on the positive $y$-axis at $(0, y)$. Express the area of the triangle as a function of $x$.
3. Express the volume $V$ of a sphere as a function of its surface area $S$. If the surface area doubles, how does the volume change?
4. A rectangle is inscribed in a circle of radius 2 . Let $P=(x, y)$ be the point in Quadrant I that is a vertex of the rectangle and is on the circle.
(a) Express the area of the rectangle as a function of $x$.
(b) Express the perimeter of the rectangle as a function of $x$.

5. A Norman window has the shape of a rectangle surmounted by a semicircle, as shown in the figure. A Norman window with perimeter 30 ft is to be constructed. Find a function that models the area of the window as a function of $x$.

