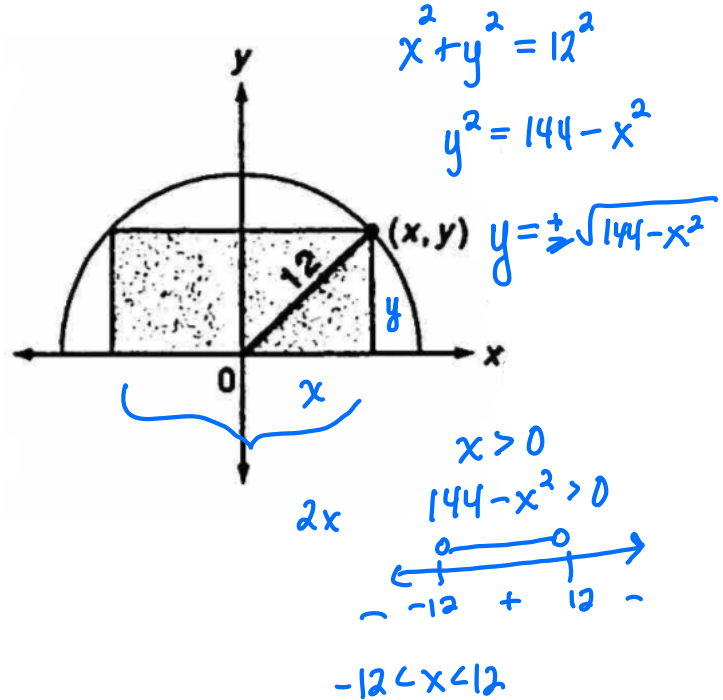


- 1. A rectangle is inscribed in a semicircle of radius 12 as shown. Express the area of the rectangle as a function of x .

$$A = lw$$

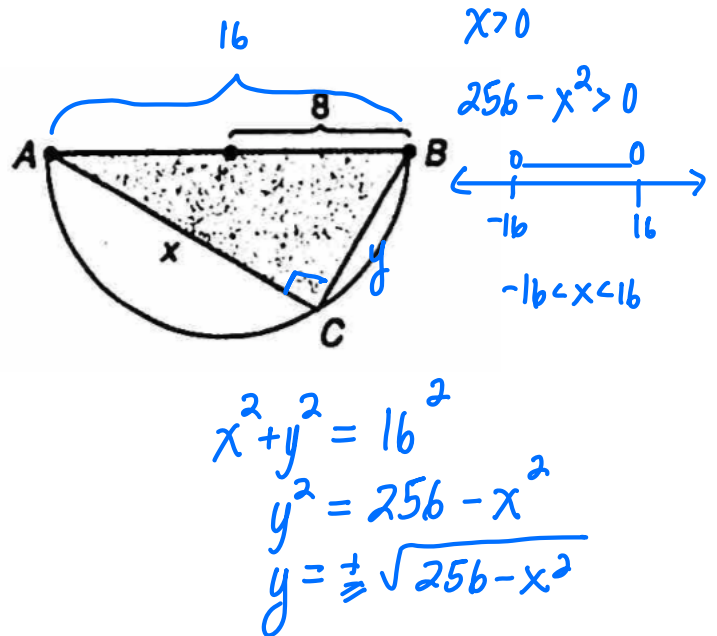
$$A(x) = 2x \cdot \sqrt{144 - x^2}, \quad 0 < x < 12$$



- 2. Triangle ABC is inscribed in a semicircle of radius 8 so that one of its sides coincides with a diameter. Express the area of the triangle as a function of $x = AC$.

$$A = \frac{1}{2}bh$$

$$A(x) = \frac{1}{2}x \cdot \sqrt{256 - x^2}, \quad 0 < x < 16$$



3. $ABCD$ is an isosceles trapezoid in which sides AB and DC are parallel. Express the area of the trapezoid as a function of altitude h .

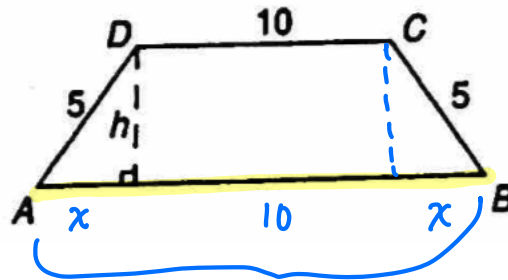
$$A = \frac{1}{2}h(b_1 + b_2)$$

$$A(h) = \frac{1}{2}h(10 + 10 + 2\sqrt{25 - h^2})$$

$$A(h) = \frac{1}{2}(20 + 2\sqrt{25 - h^2})$$

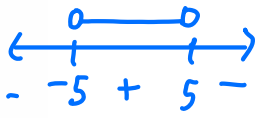
$$A(h) = 10 + \sqrt{25 - h^2}$$

$$0 < h < 5$$



$$h > 0$$

$$25 - h^2 > 0$$



$$-5 < x < 5$$

$$x^2 + h^2 = 5^2$$

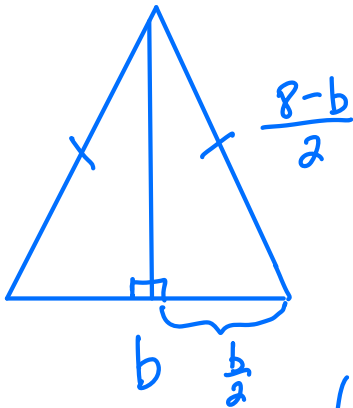
$$x^2 = 25 - h^2$$

$$x = \pm \sqrt{25 - h^2}$$

$$10 + 2x$$

$$10 + 2\sqrt{25 - h^2}$$

4. An isosceles triangle has a perimeter of 8cm. Express the area A of the triangle as a function of the length b of the base of the triangle.



$$\text{leg} = \frac{8-b}{2}$$

$$A = \frac{1}{2}bh$$

$$A(b) = \frac{1}{2}b \cdot (2\sqrt{4-b})$$

$$A(b) = b\sqrt{4-b}$$

$$0 < b < 4$$

$$\left(\frac{b}{2}\right)^2 + h^2 = \left(\frac{8-b}{2}\right)^2$$

$$\frac{b^2}{4} + h^2 = \frac{(8-b)^2}{4}$$

$$h^2 = \frac{(8-b)^2}{4} - \frac{b^2}{4}$$

$$h^2 = \frac{(8-b)^2 - b^2}{4}$$

$$h = \pm \sqrt{\frac{(8-b)^2 - b^2}{4}}$$

$$h = \sqrt{\frac{64 - 16b + b^2 - b^2}{4}}$$

$$h = \sqrt{\frac{16(4-b)}{4}}$$

$$h = \sqrt{4(4-b)} = 2\sqrt{4-b}$$

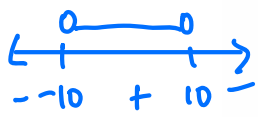
$$b > 0$$

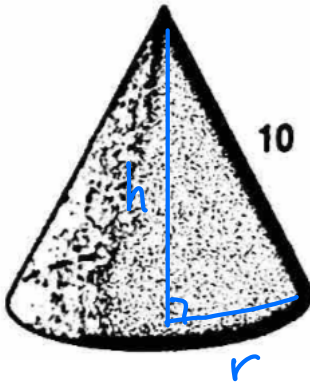
$$4 - b > 0$$

$$-b > -4$$

$$b < 4$$

5. The figure shows a right circular cone in which r is the radius of the base, and the slant height is 10. Express the volume of the cone as a function of r .

$$r > 0$$
$$100 - r^2 > 0$$

$$-10 < r < 10$$



$$V = \frac{1}{3} \pi r^2 h$$
$$V(r) = \frac{1}{3} \pi r^2 \cdot \sqrt{100 - r^2}, \quad 0 < r < 10$$

$$r^2 + h^2 = 10^2$$
$$h^2 = 100 - r^2$$
$$h = \pm \sqrt{100 - r^2}$$