

Name: _____
PC: Decomposition of Functions

Date: _____
Ms. Loughran

Do Now:

1.

For each function h given below, decompose h into the composition of two functions f and g so that $h = f \circ g$. $= f(g(x))$

(a) $h(x) = (x + 5)^2$

$$g(x) = x + 5$$
$$f(x) = x^2$$

(b) $h(x) = \sqrt[3]{5x^2 + 1}$

$$g(x) = 5x^2 + 1$$
$$f(x) = \sqrt[3]{x}$$

(c) $h(x) = 2^{\cos x}$

$$g(x) = \cos x$$
$$f(x) = 2^x$$

(d) $h(x) = \cos(2^x)$

$$g(x) = 2^x$$
$$f(x) = \cos x$$

(e) $h(x) = \frac{\sqrt{x^2 + 1} - 1}{\sqrt{x^2 + 1} + 1}$

$$g(x) = x^2 + 1$$
$$f(x) = \frac{\sqrt{x} - 1}{\sqrt{x} + 1}$$

$$g(x) = \sqrt{x^2 + 1}$$
$$f(x) = \frac{x-1}{x+1}$$

$$f(e(x))$$

$$f(3x) = (3x)^2 = 9x^2$$

$$\frac{a(a(x))}{a(x+1)} = x+1+1 = x+2$$

8. Express each of the following below as composites of two or more of the following:

$$a(x) = x + 1$$

$$g(x) = x^3$$

$$b(x) = x - 2$$

$$h(x) = \frac{1}{x}$$

$$e(x) = 3x$$

$$k(x) = \sqrt{x}$$

$$f(x) = x^2$$

$$(a) 3x + 1$$

$$(h) x + 2$$

$$(o) \frac{1}{\sqrt{x}}$$

$$a(e(x))$$

$$a(a(x))$$

$$h(k(x))$$

$$(b) 3x + 3$$

$$(i) x - 1$$

$$(p) \frac{1}{\sqrt{x-2}}$$

$$e(a(x))$$

$$b(a(x)) \text{ or } a(b(x))$$

$$h(k(b(x)))$$

$$(c) 3x^2$$

$$(j) x^2 - 1$$

$$(q) \frac{1}{\sqrt{x-2}}$$

$$e(f(x))$$

$$a(b(f(x))) \text{ or } b(a(f(x)))$$

$$h(b(k(x)))$$

$$(d) 9x^2$$

$$(k) 3x + 2$$

$$(r) x^{\frac{3}{2}} \xrightarrow{\text{power}} \sqrt{x^3} = \sqrt{x^3}$$

$$f(e(x)) \text{ or } e(f(x))$$

$$a(a(e(x)))$$

$$k(g(x)) \text{ or } g(k(x))$$

$$(e) (x^3 - 2)^2$$

$$(l) \sqrt{x^3 + 1}$$

$$x^{\frac{1}{3}} = \frac{x}{3}$$

$$f(b(g(x)))$$

$$k(a(g(x)))$$

$$\text{hint: create } \frac{3}{x} \text{ first}$$

$$(f) 9x + 3$$

$$(m) \sqrt{x+1}$$

$$3 \cdot \frac{1}{x}$$

$$e(a(e(x)))$$

$$k(a(x))$$

then flip it

$$(g) \frac{1}{\sqrt{x^2 + 1}}$$

$$(n) \sqrt{x} + 1$$

$$h(e(h(x)))$$

$$h(k(a(f(x))))$$

$$a(k(x))$$

Homework 10-13

Name: Kay
 PC: Decomposition Homework

Date: _____
 Ms. Loughran

For 1 – 4, express the function in the form $f \circ g \circ h$.

1. $F(x) = \sqrt[3]{\sqrt{x-1}}$

$$\begin{aligned} h(x) &= \sqrt{x} \\ g(x) &= x-1 \\ f(x) &= \sqrt[3]{x} \end{aligned}$$

2. $F(x) = (4 + \sqrt[3]{x})^9$

$$\begin{aligned} h(x) &= \sqrt[3]{x} \\ g(x) &= 4+x \\ f(x) &= x^9 \end{aligned}$$

3. $F(x) = \frac{2}{(3+\sqrt{x})^2}$

$$\begin{aligned} h(x) &= 3+\sqrt{x} \\ g(x) &= x^2 \\ f(x) &= \frac{2}{x} \end{aligned}$$

4. $F(x) = \sqrt[4]{x^3 + 9}$

$$\begin{aligned} h(x) &= x^3 \\ g(x) &= x+9 \\ f(x) &= \sqrt[4]{x} \end{aligned}$$

5. Find the functions f and g so that $h(x) = (f \circ g)(x)$

(a) $h(x) = (x-1)^3 - 2$

$$g(x) = x-1, \quad f(x) = x^3 - 2$$

(b) $h(x) = 2(x+1)^2 + 3$

$$g(x) = x+1, \quad f(x) = 2x^2 + 3$$

(c) $h(x) = \frac{x+1}{x+2}$

$$g(x) = x+1, \quad f(x) = \frac{x}{x+1}$$

6. Find the functions f , g and h so that $F(x) = (f \circ g \circ h)(x)$

$$F(x) = \sqrt{(x^2 - 3x)^5}$$

$$h(x) = x^2 - 3x$$

$$g(x) = x^5$$

$$f(x) = \sqrt{x}$$

Remember these answers are not unique. You may have come up with other answers that work.