A rational expression is a ratio of polynomials. A rational expression is said to be undefined if its denominator is zero.

1. For what value(s) of x does the expression have no meaning?

(a)
$$\frac{7}{x-3}$$

(b)
$$\frac{12}{x+8}$$

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$$\frac{7}{x-3}$$
 (b) $\frac{12}{x+8}$ (c) $\frac{x-3}{x^2-16}$ (d) $\frac{x-2}{x^2+4}$

(d)
$$\frac{x-2}{x^2+4}$$

2. Find the value(s) of the variable for which each rational expression is not defined.

(a)
$$\frac{x^2-49}{2x^2-4x}$$

(b)
$$\frac{5}{c^2 - 25}$$

(c)
$$\frac{x-3}{x^2+9}$$

(a)
$$\frac{x^2 - 49}{2x^2 - 4x}$$
 (b) $\frac{5}{c^2 - 25}$ (c) $\frac{x - 3}{x^2 + 9}$ (d) $\frac{6}{3x^2 - 8x + 4}$

Simplify each expression.

$$3. \ \frac{x^2 + 6x}{x}$$

$$8. \ \frac{x^2 - x - 6}{3x^2 - 15x + 18}$$

4.
$$\frac{x^2}{x^2 + 3x}$$

9.
$$\frac{y^2 - 3y - 18}{2y^2 + 5y + 3}$$

$$5. \ \frac{5b^2 - 5ab}{2a^2 - 2ab}$$

10.
$$\frac{x^2 - y^2}{x^2 - 6y - xy + 6x}$$

6.
$$\frac{x^2 + 2x - 3}{x^2 - 1}$$

11.
$$\frac{1-x^2}{x^3-1}$$

$$7. \ \frac{5x^2 - 15x}{27x - 3x^2}$$

12.
$$\frac{x^2 + 2x + xy + 2y}{x^2 + 4x + 4}$$

13.
$$\frac{x^3 + 27}{x^3 - 3x^2 + 9x}$$

Steps for Simplifying Rational Expressions:

- 1. Completely factor the numerator and denominator
- 2. Cancel common factors

*Note
$$\frac{a-b}{b-a} = -1$$

Don't forget to write restrictions.