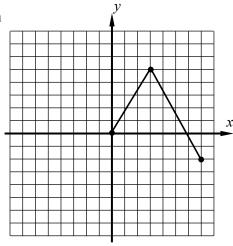
Name:	Date:
PCH Even and Odd Functions	

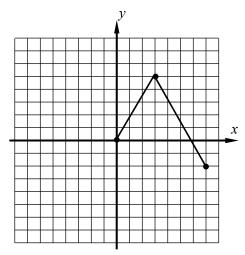
Do Now:

Consider the **partial graph** of the function f(x) shown twice below. Sketch the other half of the function if in (a) f(x) is **even** and in (b) f(x) is **odd**. The three coordinate pairs are listed to help you plot.

(a) even



(b) odd



Let *f* be a function.

f is even if f(-x) = f(x) for all x in the domain of f

f is odd if f(-x) = -f(x) for all x in the domain of f

The graph of an even function is symmetric with respect to the y-axis.

The graph of an odd function is symmetric with respect to the origin.

## Examples:

Determine whether the functions are even, odd, or neither even nor odd.

1. 
$$f(x) = x^5 + x$$

2. 
$$g(x) = 1 - x^4$$

1. 
$$f(x) = x^5 + x$$
 2.  $g(x) = 1 - x^4$  3.  $h(x) = 2x - x^2$ 

4. 
$$f(x) = 3x^3 + 2x^2 + 1$$
 5.  $g(x) = x + \frac{1}{x}$ 

$$5. \quad g(x) = x + \frac{1}{x}$$

6. 
$$h(x) = x^4 - 4x^2$$

## **Exercises**

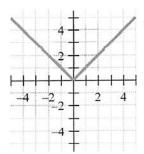
- 1. If a function is even, its graph is symmetric with respect to the \_\_\_\_\_\_

  This also means that f(-x) = \_\_\_\_\_\_
- 2. If a function is odd, its graph is symmetric with respect to the \_\_\_\_\_\_

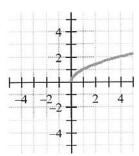
  This also means that f(-x) =\_\_\_\_\_

Determine whether each function graphed is even, odd, or neither

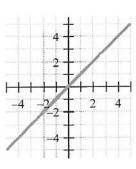
3.



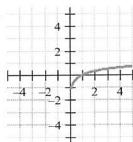
4.



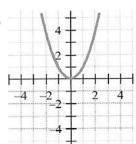
\_\_\_5.



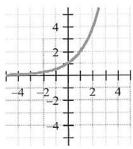
\_\_\_\_6.



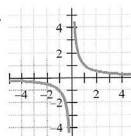
\_\_\_\_7.



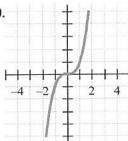
\_\_\_\_8.



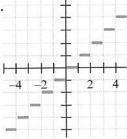
\_\_\_\_9.



\_\_\_10.



\_\_\_11.



Determine algebraically whether each of the following functions is even, odd or neither.

12. 
$$f(x) = 4x + 5$$

13. 
$$f(x) = x^3 - x$$

14. 
$$f(x) = x^2 - 6$$

15. 
$$f(x) = x^3 - x - 2$$

16. 
$$f(x) = \frac{x^4 - x}{x^5 - x}$$

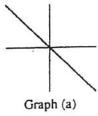
17. 
$$f(x) = \frac{x^3 - x}{x^5}$$

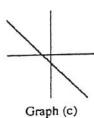
18. 
$$f(x) = (x-4)^2$$

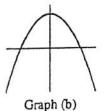
19. 
$$f(x) = x^4 - x^2 + 4$$

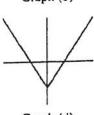
## **More Practice**

1. Indicate which of the following functions are even, which are odd, and which are neither.









Graph (d)

- 2. Algebraically, determine whether each function is odd, even, or neither.
  - a)  $f(x) = 3x^4 5x^2 + 17$

- $b) \quad f(x) = |x|$
- c)  $f(x)=12x^7+6x^3-2x$
- d)  $f(x) = 4x^3 7$

e)  $f(x)=x^2+2x+2$ 

f)  $f(x) = \frac{x^2 - 5}{2x^3 + x}$ 

1. For each of the following functions, use the definitions above to determine whether each is an even function, an odd function, both, or neither. Also, state the type of symmetry exhibited by each even and odd function.

a) 
$$y = x^4$$

$$y = \frac{1}{1 + x^2}$$

b) 
$$y = x^3 - 4x$$

$$m) y = \frac{x^2 + 6}{x}$$

c) 
$$y = x^2 + x$$

$$y = \frac{x}{x^3 + 1}$$

$$d) \quad y = 0$$

e) 
$$y = 7$$

o) 
$$y = |x|$$

f) 
$$y = 7x$$

p) 
$$y = |x| + 2$$

$$y = 7x + 1$$

$$\mathbf{q)} \qquad \mathbf{y} = \|\mathbf{x} + \mathbf{2}\|$$

h) 
$$y = 3x^2 - 5$$

$$y = \sqrt{4 - x^2}$$

i) 
$$y = 3x^3 - 5$$

s) 
$$y = \sqrt{x}$$

$$j) \qquad y = 3x^3 - 5x$$

t) 
$$y = \sqrt[3]{x}$$

$$k) y = \frac{1}{r}$$

u) 
$$\{(-2,0), (2,0)\}$$

2. Sketch the graphs of  $y = \sin x$ ,  $y = \cos x$ , and  $y = \tan x$ . Determine which of these are even and odd.