Name:
Date: $\qquad$
PCH - Modeling with Functions

1. A rectangular piece of cardboard has dimensions of 20 cm by 70 cm . Congruent squares of $x \mathrm{~cm}$ on each side are cut from each of the 4 corners of this rectangle and the sides are folded up to form an open rectangular box. Express the volume of this box as a function of $x$.
2. A closed rectangular shaped box is $x$ units wide and 3 times as long. Let $h$ be the altitude of this box. If the total surface area of this box is 150 square units, express the volume of the box as a function of $x$.
3. The vertices of a right triangle are $(0,0),(x, 0)$, and $(0, y)$. If $(6,2)$ lies on the hypotenuse of the triangle, express the area of the triangle as a function of $x$.
4. A right triangle has one vertex on the graph of $y=7-x^{2}$, where $x>0$ at $(x, y)$, another at the origin, and the third on the positive $x$-axis at $(x, 0)$. Express the area of the triangle as function of $x$.
5. A rectangle has one corner on the graph of $y=9-x^{2}$, where $x>0$, at $(x, y)$, another corner at the origin, a third corner on the positive $x$-axis at $(x, 0)$, and a fourth corner on the positive $y$-axis at $(0, y)$. Express the area of the rectangle as function of $x$.
6. Let $P=(x, y)$ be a point on the graph of $y=\sqrt{x}$. Express the distance $d$ from $P$ to the point $(1,0)$ as a function of $x$.
7. A rectangle has a side measuring $x$ inches and a diagonal measuring 10 inches. Express the area of the rectangle as a function of $x$.
8. A water tank is in the shape of an inverted right cylindrical cone with altitude 50 feet and radius 14 feet. The tank is filled to a depth of $h$ feet. Let $x$ be the radius of the circle at the top of the water level. Express the volume of the water as a function of $x$.
9. Express the area of the shaded region as a function of $x$.

10. A wire 12 meters long is to be cut into two pieces. One piece will be shaped as an equilateral triangle and the other piece will be shaped as a circle. If $x$ represents the length of a side of the equilateral triangle, express the total area $A$ enclosed by the pieces of wire as a function of $x$.
