

Name: _____
PCH

Date: _____
Ms. Loughran

Do Now:
Factor each of the following completely.

1. $121s^2 - 66st + 9t^2$

$$(11s - 3t)^2$$

2. $u^2 - v^2 + 2v - 1$

$$\begin{aligned} &u^2 - (v^2 - 2v + 1) \\ &u^2 - (v-1)^2 \\ &(u - (v-1))(u + (v-1)) \\ &(u - v + 1)(u + v - 1) \end{aligned}$$

3. $x^{2n} - 1$

$(x^n - 1)(x^n + 1)$

we could

$(x^{\frac{n}{2}} - 1)(x^{\frac{n}{2} + 1})(x^n + 1)$

⋮

(5)

$(x^{\frac{2}{3}} - 16)$

$(x^{\frac{1}{3}} + 4)(x^{\frac{1}{3}} - 4)$

$(x^{\frac{1}{3}} + 4)(x^{\frac{1}{10}} + 2)(x^{\frac{1}{10}} - 2)$

4. $x^{2n} + 2x^n y^n + y^{2n}$

$$(x^n + y^n)^2$$

Name: _____
PCH

Date: _____
Ms. Loughran

Do Now:

Factor each of the following completely.

1. $x^6 + 5x^5 - 5x^4 - 25x^3 + 4x^2 + 20x$

$$x^5(x+5) - 5x^3(x+5) + 4x(x+5)$$

$$(x^5 - 5x^3 + 4x)(x+5)$$

$$x(x^4 - 5x^2 + 4)(x+5)$$

$$x(x^2 - 1)(x^2 - 4)(x+5)$$

$$x(x+1)(x-1)(x+2)(x-2)(x+5)$$

3. $(5x-6)^2 - (4x-3)^2$

$$(5x-6+4x-3)(5x-6-(4x-3))$$

$$(9x-9)(x-3)$$

$$9(x-1)(x-3)$$

2. $4x^8 - 61x^4 + 225 + x^4 - x^4$

$$4x^8 - 60x^4 + 225 - x^4$$

$$(2x^4 - 15)^2 - x^4$$

$$(2x^4 - x^2 - 15)(2x^4 + x^2 - 15)$$

$$(2x^2 + 5)(x^2 - 3)(2x^2 - 5)(x^2 + 3)$$

4. $3x(x+2)^{\frac{1}{3}} + 4(x+2)^{\frac{2}{3}}$

$$(x+2)^{-\frac{1}{3}}(3x + 4(x+2))$$

$$(x+2)^{-\frac{1}{3}}(7x+8)$$

$$\frac{7x+8}{(x+2)^{\frac{1}{3}}}$$

$$x \neq -2$$

Simplify:
$$\frac{(1+x^2)^{\frac{1}{2}} - x^2 (1+x^2)^{-\frac{1}{2}}}{1+x^2}$$

$$\frac{(1+x^2)^{-\frac{1}{2}} (1+x^2 - x^2)}{1+x^2}$$

$$\frac{(1+x^2)^{-\frac{1}{2}}}{1+x^2}$$

$$\frac{1}{(1+x^2)^{\frac{1}{2}} (1+x^2)} = \frac{1}{(1+x^2)^{\frac{3}{2}}}$$

Simplify:

$$\frac{3(x+2)^2(x-3)^2 - (x+2)^3(2)(x-3)}{(x-3)^4}$$

$$\frac{(x+2)^2(x-3) \left[\begin{array}{cc} 3x-9 & -2x-4 \\ 3(x-3) & -2(x+2) \end{array} \right]}{(x-3)^4}$$

$$\frac{(x+2)^2 \cancel{(x-3)} (x-13)}{(x-3)^4}$$

$$\frac{(x+2)^2 (x-13)}{(x-3)^3}$$

$x \neq 3$

$$\textcircled{9} \quad x^{3/5} + 5x^{2/5} - 3x^{1/5} - 15$$

$$x^{2/5} (x^{1/5} + 5) - 3 (x^{1/5} + 5)$$

$$(x^{2/5} - 3)(x^{1/5} + 5)$$

$$16x^4 + 16x^2y^2 + 16y^4$$

$$16(x^4 + x^2y^2 + y^4 + x^2y^2 - x^2y^2)$$

$$16 \left[(x^2 + y^2)^2 - x^2y^2 \right]$$

$$16(x^2 - xy + y^2)(x^2 + xy + y^2)$$