

PreCalculus Honors – Some Review Problems

1. Solve using the geometric definition of absolute value: $\left|7 - \frac{3}{2}x\right| < 4$

2. Solve and express your solution on a number line and in interval notation:

$$\frac{x(7-x)(2x+1)}{(x-1)^2} \geq 0$$

3. Rewrite as a piecewise function using the algebraic definition of absolute value and graph the function: $y = |4x - 1|$

4. $f(x)$ represents a linear function, $f(3) = -2$ and $f(-7) = 1$. Find an equation for $f(x)$ in standard form.

5. A property owner wants to fence a rectangular garden plot with one side adjacent to a road. The fencing next to the road must be sturdier and costs \$5 per foot, but the other sides can be fenced with fencing that costs \$3 per foot. The garden must have an area of 1200 square feet. Find a function that models the cost of fencing the garden.

6. Factor completely:

(a) $(3a + 1)^2 - 6(3a + 1) - 8$

(b) $1000x^3y^9 - 125a^{12}b^{15}$

(c) $x^4 - 15x^2 + 9$

7. Express in simplest form and set any necessary restrictions:

$$\frac{4y^2 - 9}{2y^2 - 9y - 18} \div \frac{2y^2 + y - 3}{y^2 + 5y - 6}$$

8. Find the inverse of $y = -\frac{3}{2x-3} + 5$.

9. Find the functions $f \circ g$, $g \circ f$, $f \circ f$, and $g \circ g$ and their domains.

(a) $f(x) = \sqrt{x}$ and $g(x) = \sqrt{9-x}$

(b) $f(x) = \frac{1}{\sqrt{x}}$ and $g(x) = x^2 - x - 12$